

Verification of Ants time-dependent nodal neutronics model

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07/11/2022 VTT – beyond the obvious



Outline

Background

- Benchmark descriptions and results
- Conclusions



Background

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VTT is developing a new framework for reactor modeling

- Kraken is a new computational framework for coupled calculations
 - Consists of modular solvers of neutronics, fuel behaviour and thermal hydraulics
 - Data transfer between the solvers is committed with a multiphysics driver
- Current work includes coupled calculations with Kraken and system level codes, e.g. TRACE



Ants – nodal neutronics solver

- Developed at VTT since 2017
- Object: Reduced-order core-level routine calculations with low computational cost
- Steady-state calculations have been verified for
 - Different geometries (rectangular, hexagonal and triangular)
 - Different energy group structures (two-group and multi-group)
- Time-dependent model still required verification



Nodal neutronics

- High-fidelity heterogeneous methods are not feasible for routine calculations → reduced-order methods
- Nodal methods are based on averaging fuel assemblies to homogeneous blocks, nodes
- The neutron flux is solved separately within each node and the node-wise flux solutions are coupled together with boundary conditions





$$\frac{1}{v_g(\mathbf{r})} \frac{\partial \phi_g(\mathbf{r}, t)}{\partial t} = \nabla \cdot D_g(\mathbf{r}) \nabla \phi_g(\mathbf{r}, t) - \Sigma_{\mathbf{r},g}(\mathbf{r}) \phi_g(\mathbf{r}, t) + \sum_{g'=1}^G \Sigma_{g' \to g}(\mathbf{r}) \phi_{g'}(\mathbf{r}, t) + \chi_{\mathrm{d},g}(\mathbf{r}) \sum_{k=1}^m \lambda_k(\mathbf{r}) C_k(\mathbf{r}, t) + \left(1 - \beta(\mathbf{r})\right) \chi_{\mathrm{p},g}(\mathbf{r}) \sum_{g'=1}^G \nu \Sigma_{\mathrm{f},g'}(\mathbf{r}) \phi_{g'}(\mathbf{r}, t), \frac{\partial C_k(\mathbf{r}, t)}{\partial t} = \beta_k(\mathbf{r}) \sum_{g'=1}^G \nu \Sigma_{\mathrm{f},g'}(\mathbf{r}) \phi_{g'}(\mathbf{r}, t) - \lambda_k(\mathbf{r}) C_k(\mathbf{r}, t), \quad k = 1, 2, ..., m,$$

$$\begin{aligned} \frac{1}{v_g(\mathbf{r})} \frac{\partial \phi_g(\mathbf{r},t)}{\partial t} = \nabla \cdot D_g(\mathbf{r}) \nabla \phi_g(\mathbf{r},t) - \Sigma_{\mathbf{r},g}(\mathbf{r}) \phi_g(\mathbf{r},t) \\ &+ \sum_{g'=1}^G \Sigma_{g' \to g}(\mathbf{r}) \phi_{g'}(\mathbf{r},t) + \chi_{\mathrm{d},g}(\mathbf{r}) \sum_{k=1}^m \lambda_k(\mathbf{r}) C_k(\mathbf{r},t) \\ &+ \left(1 - \beta(\mathbf{r})\right) \chi_{\mathrm{p},g}(\mathbf{r}) \sum_{g'=1}^G \nu \Sigma_{\mathrm{f},g'}(\mathbf{r}) \phi_{g'}(\mathbf{r},t), \\ &\frac{\partial C_k(\mathbf{r},t)}{\partial t} = \beta_k(\mathbf{r}) \sum_{g'=1}^G \nu \Sigma_{\mathrm{f},g'}(\mathbf{r}) \phi_{g'}(\mathbf{r},t) - \lambda_k(\mathbf{r}) C_k(\mathbf{r},t), \quad k = 1, 2, ..., m, \end{aligned}$$

$$\frac{1}{v_{g}(\mathbf{r})} \xrightarrow{\partial \phi_{g}(\mathbf{r},t)} \xrightarrow{\mathbf{\nabla} \cdot D_{g}(\mathbf{r}) \nabla \phi_{g}(\mathbf{r},t)} \xrightarrow{\Sigma_{\mathbf{r},g}(\mathbf{r}) \phi_{g}(\mathbf{r},t)} \qquad \text{Neutron leakage}$$

$$+ \sum_{g'=1}^{G} \Sigma_{g' \to g}(\mathbf{r}) \phi_{g'}(\mathbf{r},t) + \chi_{\mathrm{d},g}(\mathbf{r}) \sum_{k=1}^{m} \lambda_{k}(\mathbf{r}) C_{k}(\mathbf{r},t)$$

$$+ \left(1 - \beta(\mathbf{r})\right) \chi_{\mathrm{p},g}(\mathbf{r}) \sum_{g'=1}^{G} \nu \Sigma_{\mathrm{f},g'}(\mathbf{r}) \phi_{g'}(\mathbf{r},t),$$

$$\frac{\partial C_{k}(\mathbf{r},t)}{\partial t} = \beta_{k}(\mathbf{r}) \sum_{g'=1}^{G} \nu \Sigma_{\mathrm{f},g'}(\mathbf{r}) \phi_{g'}(\mathbf{r},t) - \lambda_{k}(\mathbf{r}) C_{k}(\mathbf{r},t), \quad k = 1, 2, ..., m,$$

$$\frac{1}{v_{g}(\mathbf{r})} \frac{\partial \phi_{g}(\mathbf{r},t)}{\partial t} = \nabla \cdot D_{g}(\mathbf{r}) \nabla \phi_{g}(\mathbf{r},t) - \Sigma_{\mathbf{r},g}(\mathbf{r}) \phi_{g}(\mathbf{r},t) + \mathbf{r} \sum_{\mathbf{r},g}(\mathbf{r}) \phi_{g}(\mathbf{r},t) + \mathbf{r} \sum_{\mathbf{r},g}(\mathbf{r}) \phi_{g}(\mathbf{r},t) + \mathbf{r} \sum_{k=1}^{G} \lambda_{k}(\mathbf{r}) C_{k}(\mathbf{r},t) + \sum_{k=1}^{G} \sum_{g' \to g}(\mathbf{r}) \phi_{g'}(\mathbf{r},t) + \chi_{\mathrm{d},g}(\mathbf{r}) \sum_{k=1}^{m} \lambda_{k}(\mathbf{r}) C_{k}(\mathbf{r},t) + \left(1 - \beta(\mathbf{r})\right) \chi_{\mathrm{p},g}(\mathbf{r}) \sum_{g'=1}^{G} \nu \Sigma_{\mathrm{f},g'}(\mathbf{r}) \phi_{g'}(\mathbf{r},t),$$

$$\frac{\partial C_{k}(\mathbf{r},t)}{\partial t} = \beta_{k}(\mathbf{r}) \sum_{g'=1}^{G} \nu \Sigma_{\mathrm{f},g'}(\mathbf{r}) \phi_{g'}(\mathbf{r},t) - \lambda_{k}(\mathbf{r}) C_{k}(\mathbf{r},t), \quad k = 1, 2, ..., m,$$



$$\begin{aligned} \frac{1}{v_g(\mathbf{r})} \frac{\partial \phi_g(\mathbf{r},t)}{\partial t} &= \nabla \cdot D_g(\mathbf{r}) \nabla \phi_g(\mathbf{r},t) - \Sigma_{\mathbf{r},g}(\mathbf{r}) \phi_g(\mathbf{r},t) \\ &+ \sum_{g'=1}^G \Sigma_{g' \to g}(\mathbf{r}) \phi_{g'}(\mathbf{r},t) + \chi_{\mathrm{d},g}(\mathbf{r}) \sum_{k=1}^m \lambda_k(\mathbf{r}) C_k(\mathbf{r},t) \\ &+ \left(1 - \beta(\mathbf{r})\right) \chi_{\mathrm{p},g}(\mathbf{r}) \sum_{g'=1}^G \nu \Sigma_{\mathrm{f},g'}(\mathbf{r}) \phi_{g'}(\mathbf{r},t), \end{aligned}$$

$$\begin{aligned} & \text{Delayed neutrons} \\ &\text{born from precursor} \\ &\text{decay} \end{aligned}$$

$$\frac{1}{v_{g}(\mathbf{r})} \frac{\partial \phi_{g}(\mathbf{r},t)}{\partial t} = \nabla \cdot D_{g}(\mathbf{r}) \nabla \phi_{g}(\mathbf{r},t) - \Sigma_{\mathbf{r},g}(\mathbf{r}) \phi_{g}(\mathbf{r},t) + \sum_{g'=1}^{G} \Sigma_{g' \to g}(\mathbf{r}) \phi_{g'}(\mathbf{r},t) + \chi_{\mathrm{d},g}(\mathbf{r}) \sum_{k=1}^{m} \lambda_{k}(\mathbf{r}) C_{k}(\mathbf{r},t) + (1 - \beta(\mathbf{r})) \chi_{\mathrm{p},g}(\mathbf{r}) \sum_{g'=1}^{G} \nu \Sigma_{\mathrm{f},g'}(\mathbf{r}) \phi_{g'}(\mathbf{r},t),$$
Prompt neutrons from fission
$$\frac{\partial C_{k}(\mathbf{r},t)}{\partial t} = \beta_{k}(\mathbf{r}) \sum_{g'=1}^{G} \nu \Sigma_{\mathrm{f},g'}(\mathbf{r}) \phi_{g'}(\mathbf{r},t) - \lambda_{k}(\mathbf{r}) C_{k}(\mathbf{r},t), \quad k = 1, 2, ..., m,$$

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Decay of precursors

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Ants uses AFEN and FENM methods to solve the time-dependent diffusion equation in each node separately



Benchmark descriptions and results

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- 1. One-point kinetics problem:
 - One-point one-group core with no delayed neutrons with a step absorption cross section change.
 - Analytical solution available for time-integration method verification
- 2. TWIGL problem:
 - 2D core with a ramp and a step change of absorption cross section.
- 3. LMW problem:
 - 3D simplified PWR core with moderate control rod movements.
- 4. AER-DYN-001 problem:
 - Rod ejection transient with SCRAM in a VVER-440 hexagonal core.
- 5. AER-DYN-002 problem:
 - Rod ejection transient with Doppler feedback effect in a VVER-440 hexagonal core.
- 6. LRA problem:
 - Rod drop transient in a BWR core with a simple Doppler feedback mechanism.

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The LMW problem geometry

Fuel materials 1 and 3 Control rod material 2 Reflector material 4



Radial geometry of the quarter-core model



Axial geometry of the quarter-core model in the initial state (left) and final state (right)

The LMW transient problem

- Includes movements of two control rod groups
- At 0 s, control rod group 1 is withdrawn with 3 cm/s velocity
 Control rod group 1
- At 7.5 s, control rod group 2 is inserted at 3 cm/s velocity and stopped at 60 cm elevation from the bottom of the core





-0.20

The LMW initial power distribution





Relative difference between Ants and MGRAC



The LMW transient results





The LMW final power distribution



Ants power distribution



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The LRA BWR rod-drop problem

Rod indicated by CR drops with 150 cm/s velocity
Fuel temperature obeys equation

$$\frac{\partial T_{\rm f}^k(t)}{\partial t} = \alpha \sum_{g=1}^2 \Sigma_{{\rm f},g}^k \phi_g^k({\bf r},t)$$



Doppler feedback effect based on fuel temperature changes is given as

$$\Sigma_{\mathrm{a},1}^{k}(t) = \Sigma_{\mathrm{a},1}^{k,0} \left[1 + \gamma_{\mathrm{d}} \left(\sqrt{T_{\mathrm{f}}^{k}(t)} - \sqrt{T_{\mathrm{f}}^{0}} \right) \right]$$



-0.40

-0.30

0.20 😥

difference

-0.10 Belative -0.20

-0.30

-0.40

The LRA problem – initial power distribution



Relative difference between Ants and QUANDRY

VTT

The LRA problem – transient





The LRA problem – final power distribution



Absolute difference between Ants and POLCA-T

The LRA problem – transient

Code	Ants	QUANDRY	CONQUEST
Mesh size (cm^3)	$15 \times 15 \times 15$	$15(30) \times 15(30) \times 30$	$15 \times 15 \times 30$
Number of time steps	410	410	410
Time at first peak (s)	0.907	0.907	0.905
Power at first peak (W/cm^3)	5550	5739	5390
Time at first minimum (s)	1.00	0.988	~ 1.0
Power at first minimum (W/cm^3)	120	109	~ 100
Time at second peak (s)	1.42	1.44	1.44
Power at second peak (W/cm^3)	353	412	431





Conclusions

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- The verification cases included different geometries, transient events and levels of feedback effects. However, all cases included two-group energy structure
- The Ants results showed good agreement with other nodal solutions
- Multi-group time-dependent capability is still to be tested with, e.g., the PWR MOX/UO2 Core Transient Benchmark
- Current work includes coupled time-dependent calculation with other Kraken-solvers



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